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G. VENKATASWAMY NAIDU COLLEGE (AUTONOMOUS), KOVILPATTI – 628 502.



UG DEGREE END SEMESTER EXAMINATIONS - APRIL 2025.

(For those admitted in June 2023 and later)

PROGRAMME AND BRANCH: B.SC., PHYSICS/CHEMISTRY

SEM	CATEGORY	COMPONENT	COURSE CODE	COURSE TITLE
II	PART - III	ELECTIVE GENERIC-2	U23MA2A2	VECTOR CALCULUS

Date & Session: 03.05.2025/FN

Time: 3 hours

Maximum: 75 Marks

Course Outcome	Bloom's K-level	Q. No.	SECTION – A (10 X 1 = 10 Marks) Answer <u>ALL</u> Questions.
CO1	K1	1.	A physical quantity which has only magnitude is _____. a) scalar b) vector c) matrix d) set
CO1	K2	2.	Discuss a physical quantity both magnitude and direction is named as _____. a) scalar b) vector c) matrix d) set
CO2	K1	3.	A vector \mathbf{F} is called harmonic vector if a) $\nabla^2 R = f$ b) $\nabla^2 \mathbf{F} = 0$ c) $\mathbf{F} = 0$ d) None of these
CO2	K2	4.	If $\nabla \times \mathbf{V} = 0$. Then \mathbf{V} is said to be _____ vector a) irrotational b) variable c) solenoidal d) constant
CO3	K1	5.	If a vector field \mathbf{F} is such that $\mathbf{F} = \nabla \phi$ then \mathbf{F} said to be _____. a) variable b) conservative c) Parallel field d) None
CO3	K2	6.	If $\mathbf{F} = 2x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$ then $\nabla \cdot \mathbf{F} =$ a) 0 b) 2 c) 1 d) 4
CO4	K1	7.	If $\mathbf{F} = x\mathbf{i} + y\mathbf{j} + az\mathbf{k}$ is solenoidal then 'a' is ----- a) 0 b) 2 c) -2 d) 1
CO4	K2	8.	The necessary and sufficient condition that $\int \mathbf{f} \cdot d\mathbf{r}$ be independent of the path is _____. a) $\mathbf{F} = \nabla \phi$ b) $\nabla \times \mathbf{F} = 0$ c) $\nabla \cdot \mathbf{F} = 0$ d) 3
CO5	K1	9.	Green's theorem in space is same as -----theorem a) Stoke's b) Gauss convergence c) Gauss divergence d) Fermat's
CO5	K2	10.	By Stoke's theorem if $\mathbf{r} = x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$ then $\iint (\nabla \times \mathbf{r}) \cdot \mathbf{n} \cdot d\mathbf{s} =$ a) -1 b) 1 c) none d) 0
Course Outcome	Bloom's K-level	Q. No.	SECTION – B (5 X 5 = 25 Marks) Answer <u>ALL</u> Questions choosing either (a) or (b)
CO1	K3	11a.	Find the directional derivative of $\phi = xy^2 + yz^3$ at the point (2,-1,1) in the direction of $\mathbf{i} + 2\mathbf{j} + 2\mathbf{k}$
CO1	K3	11b.	(OR) Find the unit normal to the surface $x^3 - xyz + z^3 = 1$ at (1,1,1)

CO2	K3	12a.	Find the curl (curl F) at the point (1,1,1) if $F=x^2y\mathbf{i}+xz\mathbf{j}+2yz\mathbf{k}$ (OR)
CO2	K3	12b.	P.T $\text{div } \mathbf{r} = 3$ and $\text{curl } \mathbf{r} = 0$ when \mathbf{r} is the position vector of a point (x,y,z) in space.
CO3	K4	13a.	Evaluate $\int \mathbf{f} \cdot d\mathbf{r}$ over C where $\mathbf{f}=(x^2+y^2)\mathbf{i} + (x^2-y^2)\mathbf{j}$ and c is the curve $y=x^2$ joining (0,0) and (1,1) (OR)
CO3	K4	13b.	If $\mathbf{f} = x^2\mathbf{i}-xy\mathbf{j}$ and C is the straight line joining the points (0,0) and (1,1) Evaluate integral over $\int \mathbf{f} \cdot d\mathbf{r}$ over C
CO4	K4	14a.	Explain the volume of the sphere $x^2+y^2+z^2=a^2$ as a volume integral (OR)
CO4	K4	14b.	Evaluate by using stoke's Theorem $\int yzdx + zx dy + xy dz$ where C is the curve $X^2 + Y^2 = 1, Z= Y^2$
CO5	K5	15a.	using green's Theorem, Evaluate $\int (xy-x^2)dx+x^2 y dy$ along the closed curve C formed by $y=0, x = 1$, and $y = x$ (OR)
CO5	K5	15b.	State the Gauss divergence Theorem.

Course Outcome	Bloom's K-level	Q. No.	<p align="center">SECTION – C (5 X 8 = 40 Marks) Answer ALL Questions choosing either (a) or (b)</p>
CO1	K3	16a.	Find the equation of the (i)Tangent plane (ii)Normal line to the surface $xyz=4$ at the point (1,2,2) (OR)
CO1	K3	16b.	Find the angle between the surfaces $x^2+y^2+z^2=29$ and $x^2+y^2+z^2+4x-6y-8z-47=0$ at (4,-3,2)
CO2	K4	17a.	P.T the curl ($\mathbf{r} \times \mathbf{a}$) = $-2\mathbf{a}$ where \mathbf{a} is a constant vector (OR)
CO2	K4	17b.	P.T $\text{div}(\mathbf{r}^n \mathbf{r})=(n+3)\mathbf{r}^n$. Deduce that $\mathbf{r}^n \mathbf{r}$ is a solenoidal iff $n=-3$
CO3	K4	18a.	Find the workdone by the force $\mathbf{F}=3xy\mathbf{i}-5z\mathbf{j}+10x\mathbf{k}$ along $x=t^2, y=2t^2, z=t^3$ from $t=1$ to $t=2$ (OR)
CO3	K4	18b.	Evaluate $\int \mathbf{f} \cdot d\mathbf{r}$ over C where $\mathbf{f}=(3x^2+6xy)\mathbf{i} + (3x^2 - y^2) \mathbf{j}$ along the curve $y=2x$ joining the points(0,0), (1,2)
CO4	K5	19a.	Evaluate $\int_0^{\log x} \int_0^x \int_0^{x+y} e^{x+y+z} dzdydx$ (OR)
CO4	K5	19b.	Justify green's theorem for the function $\mathbf{f}=(x^2+y^2)\mathbf{i}-2xy\mathbf{j}$ and the curve c is the rectangle in the xy plane bounded by $y=0, y=b, x=0, x=a$
CO5	K5	20a.	Justify Stoke's theorem for the function $\mathbf{f}= y^2\mathbf{i}+y\mathbf{j} -x z \mathbf{k}$ and s is the upper half of the sphere $x^2+y^2+z^2=a^2$ and $z \geq 0$ (OR)
CO5	K5	20b.	Justify Gauss divergence theorem for the function $\mathbf{f}=y\mathbf{i}+x\mathbf{j}+z^2\mathbf{k}$ for the cylindrical region S is given by $x^2+y^2=a^2, z=0$ and $z=h$